

# Applied Deep Learning

## Chapter 8: Representation and Generation

Ali Bereyhi

`ali.bereyhi@utoronto.ca`

Department of Electrical and Computer Engineering  
University of Toronto

Winter 2026

# Generating New Data via AEs

*Let's keep the track of their applications*

- ① *Compression*
- ② *Finding a sparse representation of data*
- ③ *Denoising*
- ④ *Data Generation*

↳ We intend to generate a *new sample* by our *decoder* from a *seed*

↳ for instance we generate a *random seed* and give it to *decoder*

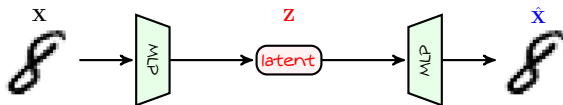
↳ the decoder returns *an image* which was *not* in the dataset

+ *That sounds crazy!*

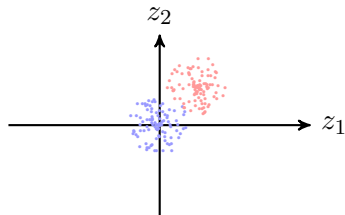
- *Well! It's not as crazy as it sounds*

## Looking into *Latent Space*

Let's get back to our **MNIST example**: assume that we set the dataset to only contain images of **handwritten 1 and 8**, and train an AE to compress them into **2-dimensional latent representations**

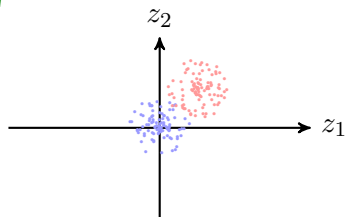


We now do a simple experiment: we pass all images of **1** and **8** that we have and mark their latent representations with **blue** and **red**



## Looking into *Latent Space*

These points show a specific behavior: *for each class, they are concentrated within an specific region*



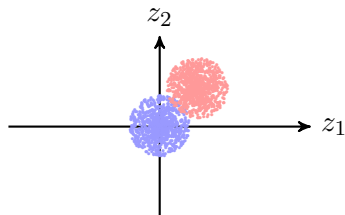
### Recall: Data Space and Distribution

In Chapter 3 we said that we can look at our dataset as a set of *samples* drawn by *some distribution* from a *data space* that contains all possible data-points

This means that we have actually lots of *other possible handwritten 1 and 8* that are not available in our dataset!

## Looking into *Latent Space*

- + *What happens if we send all of them through our AE?*
- Well! We can't say, as we have no access to them, but we may guess!



They are probably some *compact regions*

we call the union of those regions the *latent space*

Similar to data space, we *cannot* access it! We just *imagine* it!

# First Try for Generating Data

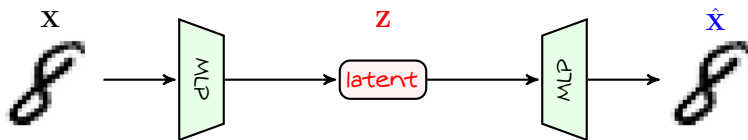
We could use this behavior to generate a new data

- We sample *a new point* in the region that we *guess* is the *latent space*
- We send this sample over *the decoder* of AE: if we are *lucky*
  - ↳ This sample is *latent representation* of a data-point that is *out of our dataset*
  - ↳ The decoder is trained well and can *reconstruct* that *data-point*
  - ↳ We have now a *data-point* out of our dataset

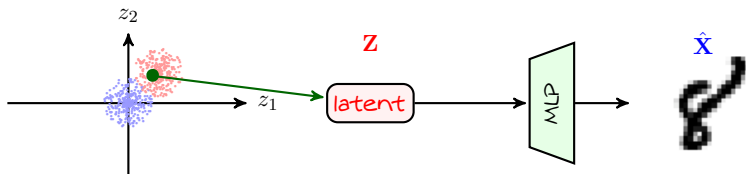
We have generated data out of some random *seed*  $\equiv$  *latent sample*

# First Try for Generating Data

We first train



We then sample the latent space



## Drawbacks of Generation via Vanilla AEs

Even though the idea seems to be **intuitive**: it turns out that it does **not** work very well when we use **basic AE architectures**

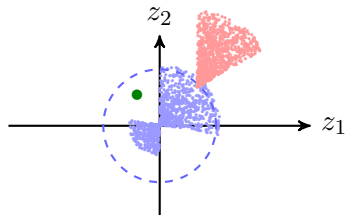
- Frequency of **invalid** generated data is quite high
  - ↳ For instance, the **decoder** returns an image which is **not** a digit
- This is **not** due to **bad training**: it happens even if AE **compresses perfectly**

---

The main reason is our significant **lack of knowledge** about **latent space**

- We guessed that **latent space** is compact and **smoothly shaped**
  - ↳ Apparently, this is **not** the case!
- By **extensive** experimental investigations, we could see
  - ↳ **Latent space** can be **extremely asymmetric**
  - ↳ It can be **hugely discontinuous**

# Drawbacks of Generation via *Vanilla* AEs



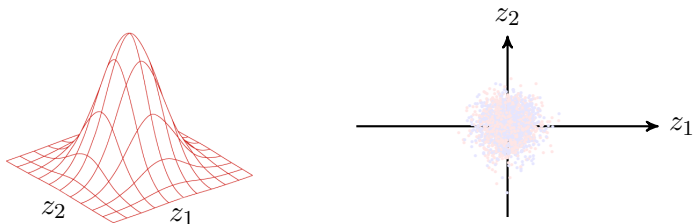
When we sample from the *postulated latent space*

- *with high chance* we could *sample* from a region *out of true latent space*
    - ↳ We hence send a *compressed* version of *invalid* image
  - *decoder returns an invalid data-point!*
- + *How can we resolve this issue?*
- We may *restrict* encoder to encode into *compact* and *symmetric* region

# Generating via Variational AEs

Variational AEs apply some trick to *make sure that*

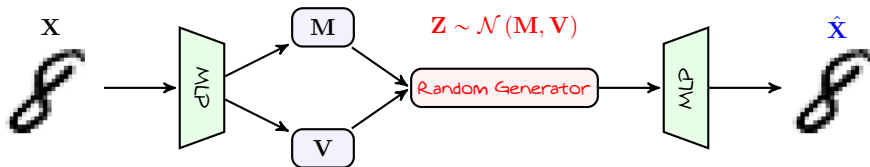
*latent representation* look like samples of a *Gaussian distribution*



Specifically, a Gaussian distribution with *mean zero* and *variance one*:  $\mathcal{N}(\mathbf{0}, \mathbf{1})$

- + How can we do it?
- Well! The trick is quite sophisticated!

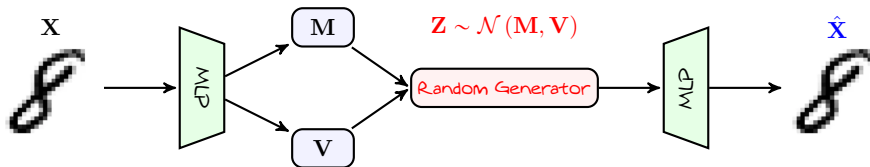
## Variational AE: Architecture



Let's formulate: say input is  $X$ , *latent representation* is  $Z$ , and  $\hat{X}$  is *output*

- We start by encoding: encoder gets  $X$  and returns
  - ↳  $M$  which is of same shape as  $Z$ : this plays the role of *mean*
  - ↳  $V$  which is of same shape as  $Z$ : this plays the role of *-variance*
- We also then generate *latent representations* at random
  - ↳  $Z$  is generated from a *Gaussian distribution*
  - ↳ *Mean* of  $Z$  is  $M$  and its *variance* is  $V$
- We give *latent representations* to the *decoder*
- We train such that *decoder* recovers the *input data*

## Variational AE: Loss



Let's specify the loss

- We need to recover from **latent representation**, i.e., we want  $\hat{\mathbf{X}} = \mathbf{X}$ 
  - ↳ Loss is proportional to the difference between  $\mathbf{X}$  and  $\hat{\mathbf{X}}$
- We want a **zero-mean** and **unit-variance** Gaussian **latent representation**
  - ↳ **Distribution** of  $\mathbf{Z}$  should be  $\mathcal{N}(\mathbf{0}, \mathbf{1})$
  - ↳ But  $\mathbf{Z}$  is generated as  $\mathcal{N}(\mathbf{M}, \mathbf{V})$
  - ↳ Loss should be **penalized** by difference between the two distribution

## Loss in VAEs

Loss is proportional to *recovery error* and *difference* between *actual* and *intended* distributions of  $\mathbf{Z}$   $\equiv$  let's call them  $p_{\mathbf{Z}}$  and  $q_{\mathbf{Z}}$ , respectively

$$\hat{R} = \mathcal{L}(\hat{\mathbf{X}}, \mathbf{X}) + \lambda \text{Div}(p_{\mathbf{Z}}, q_{\mathbf{Z}})$$

for regularizer  $\lambda$  and a difference measure  $\text{Div}(p_{\mathbf{Z}}, q_{\mathbf{Z}})$

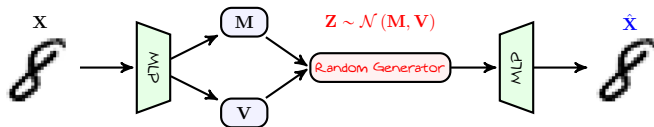
The classical choice for  $\text{Div}(p_{\mathbf{Z}}, q_{\mathbf{Z}})$  is the KL-divergence

$$\begin{aligned} \text{Div}(p_{\mathbf{Z}}, q_{\mathbf{Z}}) &= \text{KL}(p_{\mathbf{Z}} \| q_{\mathbf{Z}}) \\ &= \int p_{\mathbf{Z}}(\mathbf{Z}) \log \frac{p_{\mathbf{Z}}(\mathbf{Z})}{q_{\mathbf{Z}}(\mathbf{Z})} d\mathbf{Z} = F(\mathbf{M}, \mathbf{V}) \end{aligned}$$

So, we basically train by minimizing

$$\hat{R} = \mathcal{L}(\hat{\mathbf{X}}, \mathbf{X}) + \lambda F(\mathbf{M}, \mathbf{V})$$

# Training VAEs



Let's see how training looks: say we are training with single sample  $X$

- Pass forward  $X$  through encoder and decoder
- Backpropagate by first computing  $\nabla_{\hat{X}} \hat{R}$ 
  - ↳ Backpropagate till the **latent space**
  - ↳ At the **bottleneck**, we need to compute  $\nabla_M \hat{R}$  and  $\nabla_V \hat{R}$

$$\nabla_M \hat{R} = \underbrace{\nabla_{\hat{X}} \hat{R} \circ \nabla_M \hat{X}}_{\text{computed by Backpropagation}} + \lambda \nabla_M F(M, V)$$

- ↳ Start from  $\nabla_M \hat{R}$  and  $\nabla_V \hat{R}$  backpropagate till input
- Update weights and go for the next round

## VAEs: Final Remarks

### Attention!

We have skipped *too much details* to make it very simple: the concrete approach to understand VAEs is to

- 1 Start with looking at the NNs as machines that realize distributions
- 2 Get to the problem of *Variational Inference*
- 3 Develop an AE that performs *Variational Inference*

We then end up with VAEs

The above approach will be taken in the course *Generative AI*

But for know: you have the *main tools* to *implement* a VAE

- ↳ You may just be unsure about *some details*, e.g.,
  - ↳ Why particular expressions are defined that way?!
- ↳ You can find the answers in the course *Generative AI*

# The End!

Remember that you have the *main tools* to apply *deep learning*

- ↳ Always search for the *main three components*
  - ↳ *Model, Dataset and Loss*
- ↳ Always imagine how to *backpropagate* over the architecture
- ↳ You got into new challenges?
  - ↳ Search *online* 😊
  - ↳ Reach out to me! I would be more than happy!

---

Next in line . . .

- ↳ *This Summer Semester*
  - ↳ *Generative AI*
- ↳ *Next Fall Semester*
  - ↳ *Creative Applications of NLP*
  - ↳ *Reinforcement Learning*