

Applied Deep Learning

Chapter 8: Representation and Generation

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Generating New Data via AEs

Let's keep the track of their applications

- ① *Compression*
- ② *Finding a sparse representation of data*
- ③ *Denoising*
- ④ *Data Generation*

↳ We intend to generate a *new sample* by our *decoder* from a *seed*

↳ for instance we generate a *random seed* and give it to *decoder*

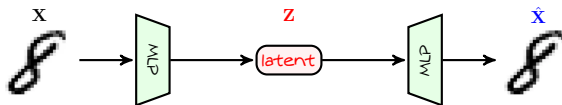
↳ the decoder returns *an image* which was *not* in the dataset

+ *That sounds crazy!*

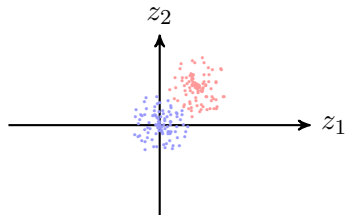
- *Well! It's not as crazy as it sounds*

Looking into Latent Space

Let's get back to our **MNIST example**: assume that we set the dataset to only contain images of **handwritten 1 and 8**, and train an AE to compress them into **2-dimensional latent representations**

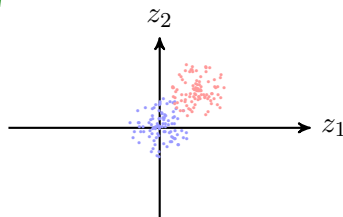


We now do a simple experiment: we pass all images of **1** and **8** that we have and mark their latent representations with **blue** and **red**



Looking into *Latent Space*

These points show a specific behavior: *for each class, they are concentrated within an specific region*



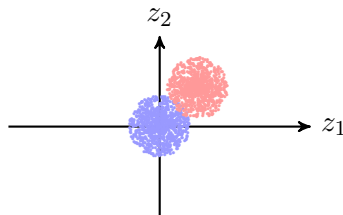
Recall: Data Space and Distribution

In Chapter 3 we said that we can look at our dataset as a set of *samples* drawn by *some distribution* from a *data space* that contains all possible data-points

This means that we have actually lots of *other possible handwritten 1 and 8* that are not available in our dataset!

Looking into *Latent Space*

- + What happens if we send all of them through our AE?
- Well! We can't say, as we have no access to them, but we may guess!



They are probably some *compact regions*

we call the union of those regions the *latent space*

Similar to data space, we *cannot* access it! We just *imagine* it!

First Try for Generating Data

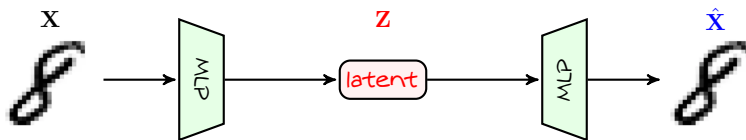
We could use this behavior to generate a new data

- We sample *a new point* in the region that we *guess* is the *latent space*
- We send this sample over *the decoder* of AE: if we are *lucky*
 - ↳ This sample is *latent representation* of a data-point that is *out of our dataset*
 - ↳ The decoder is trained well and can *reconstruct* that *data-point*
 - ↳ We have now a *data-point* out of our dataset

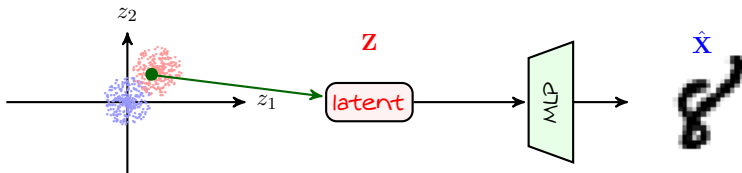
*We have generated data out of some random **seed** \equiv **latent sample***

First Try for Generating Data

We first train



We then sample the latent space



Drawbacks of Generation via Vanilla AEs

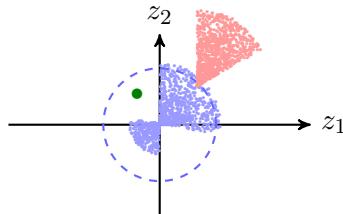
Even though the idea seems to be **intuitive**: it turns out that it does **not** work very well when we use **basic AE architectures**

- Frequency of **invalid** generated data is quite high
 - ↳ For instance, the **decoder** returns an image which is **not** a digit
- This is **not** due to **bad training**: it happens even if AE **compresses perfectly**

The main reason is our significant **lack of knowledge** about **latent space**

- We guessed that **latent space** is compact and **smoothly shaped**
 - ↳ Apparently, this is **not** the case!
- By **extensive** experimental investigations, we could see
 - ↳ **Latent space** can be **extremely asymmetric**
 - ↳ It can be **hugely discontinuous**

Drawbacks of Generation via *Vanilla* AEs



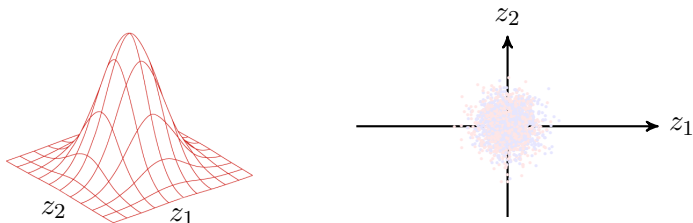
When we sample from the *postulated latent space*

- *with high chance* we could *sample* from a region *out of true latent space*
 - ↳ We hence send a *compressed* version of *invalid* image
 - *decoder returns an invalid data-point!*
- + How can we resolve this issue?
- We may *restrict* encoder to encode into *compact* and *symmetric* region

Generating via Variational AEs

Variational AEs apply some trick to *make sure that*

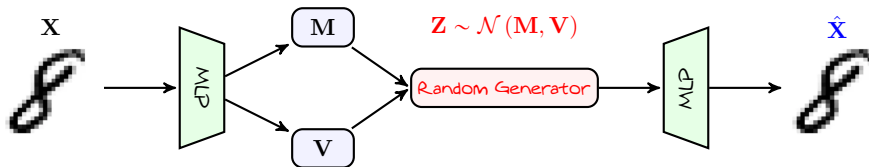
latent representation look like samples of a *Gaussian distribution*



Specifically, a Gaussian distribution with *mean zero* and *variance one*: $\mathcal{N}(\mathbf{0}, \mathbf{1})$

- + How can we do it?
- Well! The trick is quite sophisticated!

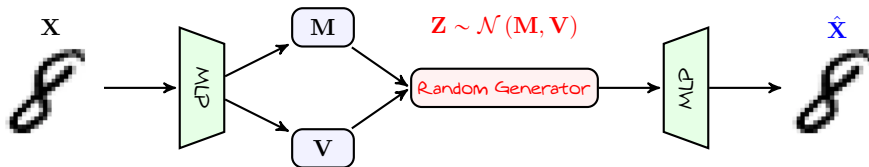
Variational AE: Architecture



Let's formulate: say input is X , **latent representation** is Z , and \hat{X} is **output**

- We start by encoding: encoder gets X and returns
 - ↳ M which is of same shape as Z : this plays the role of **mean**
 - ↳ V which is of same shape as Z : this plays the role of **-variance**
- We also then generate **latent representations** at random
 - ↳ Z is generated from a **Gaussian distribution**
 - ↳ **Mean** of Z is M and its **variance** is V
- We give **latent representations** to the **decoder**
- We train such that **decoder** recovers the **input data**

Variational AE: Loss



Let's specify the loss

- We need to recover from **latent representation**, i.e., we want $\hat{X} = X$
 - ↳ Loss is proportional to the difference between X and \hat{X}
- We want a **zero-mean** and **unit-variance** Gaussian **latent representation**
 - ↳ **Distribution** of Z should be $\mathcal{N}(0, 1)$
 - ↳ But Z is generated as $\mathcal{N}(M, V)$
 - ↳ Loss should be **penalized** by difference between the two distribution

Loss in VAEs

Loss is proportional to *recovery error* and *difference* between *actual* and *intended* distributions of $\mathbf{Z} \equiv$ let's call them $p_{\mathbf{Z}}$ and $q_{\mathbf{Z}}$, respectively

$$\hat{R} = \mathcal{L}(\hat{\mathbf{X}}, \mathbf{X}) + \lambda \text{Div}(p_{\mathbf{Z}}, q_{\mathbf{Z}})$$

for regularizer λ and a difference measure $\text{Div}(p_{\mathbf{Z}}, q_{\mathbf{Z}})$

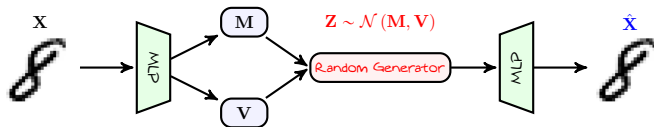
The classical choice for $\text{Div}(p_{\mathbf{Z}}, q_{\mathbf{Z}})$ is the KL-divergence

$$\begin{aligned} \text{Div}(p_{\mathbf{Z}}, q_{\mathbf{Z}}) &= \text{KL}(p_{\mathbf{Z}} \| q_{\mathbf{Z}}) \\ &= \int p_{\mathbf{Z}}(\mathbf{Z}) \log \frac{p_{\mathbf{Z}}(\mathbf{Z})}{q_{\mathbf{Z}}(\mathbf{Z})} d\mathbf{Z} = F(\mathbf{M}, \mathbf{V}) \end{aligned}$$

So, we basically train by minimizing

$$\hat{R} = \mathcal{L}(\hat{\mathbf{X}}, \mathbf{X}) + \lambda F(\mathbf{M}, \mathbf{V})$$

Training VAEs



Let's see how training looks: say we are training with single sample X

- Pass forward X through encoder and decoder
- Backpropagate by first computing $\nabla_{\hat{X}} \hat{R}$
 - ↳ Backpropagate till the **latent space**
 - ↳ At the **bottleneck**, we need to compute $\nabla_M \hat{R}$ and $\nabla_V \hat{R}$

$$\nabla_M \hat{R} = \underbrace{\nabla_{\hat{X}} \hat{R} \circ \nabla_M \hat{X}}_{\text{computed by Backpropagation}} + \lambda \nabla_M F(M, V)$$

- ↳ Start from $\nabla_M \hat{R}$ and $\nabla_V \hat{R}$ backpropagate till input
- Update weights and go for the next round

VAEs: Final Remarks

Attention!

We have skipped *too much details* to make it very simple: the concrete approach to understand VAEs is to

- 1 Start with looking at the NNs as machines that realize distributions
- 2 Get to the problem of *Variational Inference*
- 3 Develop an AE that performs *Variational Inference*

We then end up with VAEs

The above approach will be taken in the course *Generative AI*

But for know: you have the *main tools* to *implement* a VAE

- ↳ You may just be unsure about *some details*, e.g.,
 - ↳ Why particular expressions are defined that way?!
- ↳ You can find the answers in the course *Generative AI*

The End!

Remember that you have the *main tools* to apply *deep learning*

- ↳ Always search for the *main three components*
 - ↳ Model, Dataset and Loss
- ↳ Always imagine how to *backpropagate* over the architecture
- ↳ You got into new challenges?
 - ↳ Search *online* 😊
 - ↳ Reach out to me! I would be more than happy!

Next in line . . .

- ↳ This Summer Semester
 - ↳ *Generative AI*
- ↳ Next Fall Semester
 - ↳ *Creative Applications of NLP*
 - ↳ *Reinforcement Learning*